## Chapter 35 Problem 34 $^{\dagger}$

## Given

 $L = 25 \ nm = 25 \times 10^{-9} \ m$ 

## Solution

a) Find the wavelengths of the photons emitted for the transition n = 2 to n = 1.

For each part of this problem, it is necessary to calculate the energy of the transition followed by a calculation of wavelength. The energy of transition is

$$\Delta E = E_f - E_i = \frac{h^2 n_f^2}{8mL^2} - \frac{h^2 n_i^2}{8mL^2} = \frac{h^2}{8mL^2} \left(n_f^2 - n_i^2\right)$$

To eliminate repeated calculations, for this problem

$$\Delta E = \frac{(6.63 \times 10^{-34} J \cdot s)^2}{8(9.11 \times 10^{-31} kg)(25 \times 10^{-9} m)^2} \left(n_f^2 - n_i^2\right)$$
$$\Delta E = (9.65 \times 10^{-23} J) \left(n_f^2 - n_i^2\right) \tag{1}$$

Also the equation for calculating wavelength can be derived from the photon energy equation.

$$E = \frac{hc}{\lambda}$$

$$\lambda = \frac{hc}{E}$$
(2)

Since energy lost by the electron is an energy gain by the photon, the answer using equation (1) will be negative, but we will substitute in a positive value for energy into equation (2).

Now let's solve part a) by substituting in the initial and final states into equation (1).

$$\Delta E = (9.65 \times 10^{-23} J) (1^2 - 2^2) = -2.895 \times 10^{-22} J$$

Substitute this energy into equation (2) to get the wavelength

$$\lambda = \frac{(6.63 \times 10^{-34} \ J \cdot s)(3.0 \times 10^8 \ m/s)}{2.895 \times 10^{-22} \ J} = 6.87 \times 10^{-4} \ m = 0.69 mm$$

b) Find the wavelengths of the photons emitted for the transition n = 20 to n = 19.

Substitute the initial and final states into equation (1).

$$\Delta E = (9.65 \times 10^{-23} J) (19^2 - 20^2) = -3.76 \times 10^{-21} J$$

Substitute this energy into equation (2) to get the wavelength

$$\lambda = \frac{(6.63 \times 10^{-34} \, J \cdot s)(3.0 \times 10^8 \, m/s)}{3.76 \times 10^{-21} \, J} = 5.28 \times 10^{-5} \, m = 53 \, \mu m$$

c) Find the wavelengths of the photons emitted for the transition n = 100 to n = 1. Substitute the initial and final states into equation (1).

$$\Delta E = (9.65 \times 10^{-23} J) \left(1^2 - 100^2\right) = -9.65 \times 10^{-19} J$$

Substitute this energy into equation (2) to get the wavelength

$$\lambda = \frac{(6.63 \times 10^{-34} \ J \cdot s)(3.0 \times 10^8 \ m/s)}{9.65 \times 10^{-19} \ J} = 2.06 \times 10^{-7} \ m = 210 \ nm$$

<sup>&</sup>lt;sup>†</sup>Problem from Essential University Physics, Wolfson