Chapter 35 Problem 23 †

Given $L = 15 fm = 15 \times 10^{-15} m$

Solution

Find the minimum energy of an alpha particle in a uranium nucleus.

Treat the nucleas as if it were a 1D infinite square well. The energy levels of an infinite square well are given by the formula

$$E_n = \frac{n^2 h^2}{8mL^2}$$

The ground-state corresponds to n = 1. The mass of the alpha particle is four times the mass of the proton. Therefore,

$$E_1 = \frac{(1)^2 (6.63 \times 10^{-34} J \cdot s)^2}{8(4)(1.67 \times 10^{-27} kg)(15 \times 10^{-15} m)^2} = 3.66 \times 10^{-14} J$$

Converting to electron-volts gives

$$E_1 = 228 \ keV$$