Chapter 16 Problem 57 †

Given $T_{Cu} = 300 \ ^{\circ}C$ $T_{H_{2}O} = 20 \ ^{\circ}C$ $m_{H_{2}O} = 1 \ kg$ $T_f = 25 \ ^{\circ}C$ $c_{H_{2}O} = 4184 \ kcal/kg \cdot K$ $c_{Cu} = 386 \ J/kg \cdot K$

Solution

Find the mass of the copper.

Given the heat flow is transferred between the copper and water only then

$$\Delta Q_{H2O} + \Delta Q_{Cu} = 0$$

This is a statement of the conservation of heat energy. Substituting in the relationship between temperature change and heat flow gives

 $m_{H_2O}c_{H_2O} \left(T_f - T_{H_2O} \right) + m_{Cu}c_{Cu} \left(T_f - T_{Cu} \right) = 0$

Solving for the mass of copper gives us

$$m_{Cu} = \frac{-m_{H_2O}c_{H_2O} \left(T_f - T_{H_2O}\right)}{c_{Cu} \left(T_f - T_{Cu}\right)}$$
$$m_{Cu} = \frac{-(1 \ kg)(4184 \ J/kg \cdot K) \left(25 \ ^\circ C - 20 \ ^\circ C\right)}{(386 \ J/kg \cdot K) \left(25 \ ^\circ C - 300 \ ^\circ C\right)}$$
$$m_{Cu} = 0.197kg$$