

Chapter 16 Problem 50 †

Given

$$P = 10\% \text{ of } 3.0 \text{ GW}$$

$$V = 420 \text{ m}^3$$

$$T = 20 \text{ }^\circ\text{C}$$

$$c = 1 \text{ kcal/kgK}$$

$$\rho = 1000 \text{ kg/m}^3$$

Solution

Find the time for the water to reach the boiling point.

First find the amount of heat required to reach the boiling point.

$$\Delta Q = mc\Delta T$$

The mass of water is equal to its volume times density

$$\Delta Q = \rho V c \Delta T$$

$$\Delta Q = (1000 \text{ kg/m}^3)(420 \text{ m}^3)(1 \text{ kcal/kg} \cdot \text{K})(80 \text{ }^\circ\text{C})$$

$$\Delta Q = 3.36 \times 10^7 \text{ kcal}$$

Convert the kcal to joules

$$\Delta Q = 3.36 \times 10^7 \text{ kcal} \left(\frac{4184 \text{ J}}{1 \text{ kcal}} \right) = 1.41 \times 10^{11} \text{ J}$$

The heat flow is equal to the energy provided by the reactor. Since power is energy per time we have

$$P = \frac{\Delta Q}{\Delta t}$$

The power provided to warm up the water is 10% of 3 GW. This comes out to

$$P = 3 \times 10^8 \text{ W}$$

Solving for time gives us

$$\Delta t = \frac{\Delta Q}{P} = \frac{(1.41 \times 10^{11} \text{ J})}{(3.0 \times 10^8 \text{ W})} = 469 \text{ s}$$

This would be 7.81 minutes.

†Problem from Essential University Physics, Wolfson