Chapter 18 Problem 72 [†]

Given

$$\frac{\Delta W}{\Delta t} = 360~MW$$

$$\frac{\Delta U}{\Delta t} = -670~MW (\text{internal energy loss of fuel})$$

Solution

Does the turbine meet the standard of the council?

The first law of thermodynamics states

$$\Delta U = Q - W$$

When we consider the rate at which heat is released, the first law of thermodynamics can be written as

$$\frac{\Delta Q}{\Delta t} = \frac{\Delta U}{\Delta t} + \frac{\Delta W}{\Delta t}$$

Internal energy consists of the potential and kinetic energy of the molecules in the gas. During the burning of the natural gas the chemical composition changes and there is a loss of internal energy at the rate of $670 \ MW$. Since this internal energy is changed into work at a rate of $360 \ MW$, the remaining energy must be given off as a loss of heat.

$$\frac{\Delta Q}{\Delta t} = -670 \ MW + 360 \ MW = -310 \ MW$$

Since efficiency is defined as the percent of energy turned into work, the efficiency is

$$\varepsilon = \frac{360 \ MW}{670 \ MW} \times 100\% = 53.7\%$$

Since the council set minimum efficiency at 50% and the maximum thermal waste at 400~MW, the turbine meets the standard.

[†]Problem from Essential University Physics, Wolfson