

Chapter 18 Problem 30 †

Given

$$\text{flowrate} = \frac{\Delta m}{\Delta t} = 10^6 \text{ kg/s}$$

$$h = 50 \text{ m}$$

$$\text{Power} = 400 \text{ MW}$$

Solution

Find the temperature increase of the water.

Begin with the first law of thermodynamics.

$$\Delta U = Q - W$$

When we consider the rate at which energy is extracted and used, the first law of thermodynamics can be written as

$$\frac{\Delta Q}{\Delta t} = \frac{\Delta U}{\Delta t} + \frac{\Delta W}{\Delta t} \quad (1)$$

$\frac{\Delta W}{\Delta t}$ is the same as the power generated by the generator. $\frac{\Delta U}{\Delta t}$ is the rate at which potential energy is lost by the water going over the falls. Potential energy is given by $E_{\text{pot}} = mgh$. Therefore,

$$\frac{\Delta Q}{\Delta t} = \frac{\Delta m}{\Delta t} gh$$

(The negative sign is because there is a loss in height. Substituting into equation (1) and solving for $\frac{\Delta Q}{\Delta t}$ we get

$$\frac{\Delta Q}{\Delta t} = -\frac{\Delta m}{\Delta t} gh + \text{Power}$$

$$\frac{\Delta Q}{\Delta t} = -(10^6 \text{ kg/s})(9.8 \text{ m/s}^2)(50 \text{ m}) + 4.00 \times 10^8 \text{ J/s}$$

$$\frac{\Delta Q}{\Delta t} = -9.0 \times 10^7 \text{ J/s}$$

This means that every second $9.0 \times 10^7 \text{ J}$ of heat causes 10^6 kg of water to heat up. The heat capacity of water is given by

$$\Delta Q = mc\Delta T$$

Solving for temperature change gives

$$\Delta T = \frac{\Delta Q}{mc}$$

The specific heat of water is

$$c_{\text{water}} = 4184 \text{ J/kg} \cdot \text{K}$$

Therefore, the temperature change is

$$\Delta T = \frac{(9.0 \times 10^7 \text{ J})}{(10^6 \text{ kg})(4184 \text{ J/kg} \cdot \text{K})}$$

$$\Delta T = 2.15 \times 10^{-2} \text{ K} = 0.022^\circ\text{C}$$

†Problem from Essential University Physics, Wolfson