Chapter 17 Problem 45 †

Given $A = 82,000 \ km^2 = 8.2 \times 10^{10} \ m^2$ $d = 1.3 \ m$ $\rho = 917 \ kg/m^3$ $L_f = 334 \ kJ/kg$

Solution

a) Find the amount of energy required to melt all the ice on Lake Superior.

The heat required for a phase change is

$$Q = mL_f = \rho VL_f = \rho dAL_f$$

Substitute in the given values we have

$$Q = (917 \ kg/m^3)(1.3 \ m)(8.2 \times 10^{10} \ m^2)(334 \ kJ/kg)$$
$$Q = 3.26 \times 10^{16} \ kJ = 3.26 \times 10^{19} \ J$$

b) Find the average power needed to melt the ice in 3 weeks. First convert 3 weeks into seconds.

$$\Delta t = 3 \ weeks \left(\frac{7 \ days}{1 \ week}\right) \left(\frac{24 \ h}{1 \ day}\right) \left(\frac{3600 \ s}{1 \ h}\right) = 1.81 \times 10^6 \ s$$

Heat flow is just an indication of the energy that has gone into melting the ice. Power is the rate of change of energy.

$$P = \frac{\Delta Q}{\Delta t} = \frac{3.26 \times 10^{19} J}{1.81 \times 10^6 s} = 1.80 \times 10^{13} W$$
$$P = 18.0 TW$$

This may look like a large number, but if you calculate the power per square meter, you get 220 W/m^2 . This could be done by sunlight if the ice did not reflect too much of it. Also conduction from warm air over the ice will contribute to the melting too.