Chapter 16 Problem 50 †

Given

$$\begin{split} P &= 10\% \; of \; 3.0 \; GW \\ V &= 420 \; m^3 \\ T &= 20 \; ^\circ C \\ c &= 1 \; kcal/kgK \\ \rho &= 1000 \; kg/m^3 \end{split}$$

Solution

Find the time for the water to reach the boiling point.

First find the amount of heat required to reach the boiling point.

$$\Delta Q = mc\Delta T$$

The mass of water is equal to its volume times density

$$\begin{split} \Delta Q &= \rho V c \Delta T \\ \Delta Q &= (1000 \; kg/m^3) (420 \; m^3) (1 \; kcal/kg \cdot K) (80 \; ^\circ C) \\ \Delta Q &= 3.36 \times 10^7 \; kcal \end{split}$$

Convert the kcal to joules

$$\Delta Q = 3.36 \times 10^7 \ kcal \left(\frac{4184 \ J}{1 \ kcal}\right) = 1.41 \times 10^{11} \ J$$

The heat flow is equal to the energy provided by the reactor. Since power is energy per time we have

$$P = \frac{\Delta Q}{\Delta t}$$

The power provided to warm up the water is 10% of 3 GW. This comes out to

$$P = 3 \times 10^8 W$$

Solving for time gives us

$$\Delta t = \frac{\Delta Q}{P} = \frac{(1.41 \times 10^{11} J)}{(3.0 \times 10^8 W)} = 469 s$$

This would be 7.81 minutes.

[†]Problem from Essential University Physics, Wolfson