Chapter 16 Problem 37 †

Given P = 100 W $T = 3.0 \ kK = 3000 \ K$ $\sigma = 5.67 \times 10^{-8} \ W/m^2 \cdot K^4$

Solution

Find the surface area of the filament.

Stefan-Boltzmann's law states

 $P=\epsilon\sigma AT^4$

Assuming the emissivity of the filament is 1, solve for A.

$$A = \frac{P}{\sigma T^4} = \frac{100 W}{(5.67 \times 10^{-8} W/m^2 \cdot K^4)(3000 K)^4} = 2.18 \times 10^{-5} m^2$$

Convert to mm^2

$$A = (2.18 \times 10^{-5} \ m^2) \left(\frac{1000 \ mm}{1.000 \ m}\right)^2 = 21.8 \ mm^2$$