Chapter 5 Problem 66[†]

Given $E = 100 \ N/C$ $m = 2.0 \times 10^{-15} \ g = 2.0 \times 10^{-18} \ kg$ $q_e = -1.60 \times 10^{-19} \ C$

Solution

What is the magnitude and direction of the graviational and electric force on a small dust particle? What is the acceleration of the dust particle?

The graviational force will be in the downward direction (negative) and has a magnitude of

 $\vec{F}_g = m\vec{g} = (2.0 \times 10^{-18} \ kg)(9.80 \ m/s^2 - \hat{j}) = -1.96 \times 10^{-17} \ N\hat{j}$

The electric force will be in the upward direction (negative charges feel a force opposite of the direction of the electric field, which is downward) with a magnitude of

$$\vec{F}_e = q\vec{E} = (-1.60 \times 10^{-19} \ C)(-100 \ N/m\hat{j}) = 1.60 \times 10^{-17} \ N\hat{j}$$

From Newton's 2nd Law

$$\begin{split} \Sigma \vec{F} &= m \vec{a} \\ \vec{F}_g + \vec{F}_e &= m \vec{a} \\ \vec{a} &= \frac{\vec{F}_g + \vec{F}_e}{m} \\ \vec{a} &= \frac{(-1.96 \times 10^{-17} \ N\hat{j}) + (1.60 \times 10^{-17} \ N\hat{j})}{2.0 \times 10^{-18} \ kg} = \frac{-0.36 \times 10^{-17} \ N\hat{j}}{2.0 \times 10^{-18} \ kg} \\ \vec{a} &= -1.8 \ m/s^2 \hat{j} \end{split}$$

It accelerates downward with a magnitude of $1.8 m/s^2$.

 $^{^\}dagger \mathrm{Problem}$ from Univesity Physics by Ling, Sanny and Moebs (OpenStax)