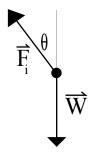
## Chapter 5 Problem 39<sup>†</sup>



## Given

 $m = 45 \ kg$   $r = 5.0 \ m$  $v = 6.3 \ m/s$ 

## Solution

a) Find the horizontal and vertical components of force exerted on the skate blades.

The free-body diagram is given above. Chose the x-coordinate to be to the right. Using Newton's  $2^{nd}$  law

$$\Sigma \vec{F} = m\vec{a}$$
$$\vec{F_i} + \vec{W} = m\vec{a}$$

Since the skater is going around a circle at constant speed the acceleration must be centripetal acceleration. The direction of this acceleration is in the -x direction. Write out the equation in unit vector notation.

$$-F_i \sin \theta \hat{i} + F_i \cos \theta \hat{j} - mg \hat{j} = -m\frac{v^2}{r}\hat{i}$$

The x-component of this equation is

$$-F_i \sin \theta = -m \frac{v^2}{r} \tag{1}$$

and the y-component of this equation is

$$F_i \cos \theta - mg = 0 \tag{2}$$

In equation (1) the horizontal component of the force on the skate blades is  $F_i \sin \theta$ . Solving for this quantity gives

$$F_h = F_i \sin \theta = m \frac{v^2}{r} = (45 \ kg) \frac{(6.3 \ m/s)^2}{(5.0 \ m)} = 357 \ N$$

The vertical component of the force on the skate blades is equal to the normal force which is the quantity  $F_i \cos \theta$ . From equation (2) this is

$$F_v = F_i \cos \theta = mg = (45 \ kg)(9.8 \ m/s^2) = 441 \ N$$

<sup>&</sup>lt;sup>†</sup>Problem from Essential University Physics, Wolfson

b) Find the angle the skater is leaning without falling over.

The angle  $\theta$  is the tangent of the opposite side (horizontal component) divided by the adjacent side (vertical component). This gives

$$\tan \theta = \frac{F_h}{F_v}$$
$$\theta = \tan^{-1} \left(\frac{F_h}{F_v}\right) = \tan^{-1} \left(\frac{357 N}{441 N}\right) = 39.0^{\circ}$$