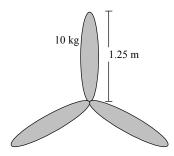
Chapter 10 Problem 53 †



Given

$$m = 10 \ kg$$
$$l = 1.25 \ m$$

Solution

a) Find the moment of inertia of the propeller.

Treating each blade as a rod, the total moment of inertia is three times the moment of inertia for a rod rotated about one end.

$$I_{tot} = 3I_{rod} = 3(\frac{1}{3}MR^2) = MR^2 = (10 \ kg)(1.25 \ m)^2$$

 $I_{tot} = 15.6 \ kg \cdot m^2$

b) Find the time to increase the angular speed from 1400 rmp to 1900 rmp due to a torque of 2700 $N \cdot m$. First convert the angular speeds into rad/s.

$$\omega_0 = \left(\frac{1400 \ rev}{min}\right) \left(\frac{2\pi \ rad}{rev}\right) \left(\frac{1 \ min}{60 \ s}\right) = 147 \ rad/s$$

$$\omega_s = \left(\frac{1900 \ rev}{rev}\right) \left(\frac{2\pi \ rad}{rev}\right) \left(\frac{1 \ min}{60 \ s}\right) = 199 \ rad/s$$

$$\omega_f = \left(\frac{1900 \ rev}{min}\right) \left(\frac{2\pi \ rad}{rev}\right) \left(\frac{1 \ min}{60 \ s}\right) = 199 \ rad/s$$

Angular acceleration is related to torque by the formula

$$\tau = I\alpha$$

Solving for angular acceleration gives

$$\alpha = \frac{\tau}{I} \tag{1}$$

Use the definition of average angular acceleration to get the time.

$$\alpha = \frac{\Delta\omega}{\Delta t}$$

$$\Delta t = \frac{\Delta\omega}{\alpha} \tag{2}$$

[†]Problem from Essential University Physics, Wolfson

Combining equation 1 and 2 gives a time of

$$\Delta t = \frac{\Delta \omega}{\tau / I} = \frac{I(\omega_f - \omega_0)}{\tau}$$

Substituting in the values gives

$$\Delta t = \frac{(15.6 \; kg \cdot m^2)(199 \; rad/s - 147 \; rad/s)}{2700 \; N \cdot m} = 0.30 \; s$$